

Composite Volumes at School Answer Key

1) Backpack + Side Pocket (rectangular prism + cylinder)

- Prism: $V = 30 \cdot 20 \cdot 45 = 27,000 \text{ cm}^3$
 - Cylinder: $V = \pi r^2 h = 3.14 \cdot 5^2 \cdot 18 = 1,413.00 \text{ cm}^3$
 - Total: $27,000 + 1,413 = 28,413 \text{ cm}^3 = \boxed{28.41 \text{ L}}$
-

2) Water Bottle Capacity (cylinder + hemisphere)

- Cylinder: $V = 3.14 \cdot 3.5^2 \cdot 22 = 846.23 \text{ cm}^3$
 - Hemisphere: $V = \frac{2}{3} \pi r^3 = \frac{2}{3} \cdot 3.14 \cdot 3.5^3 = 89.75 \text{ cm}^3$
 - Total: $846.23 + 89.75 = \boxed{935.98 \text{ cm}^3}$
-

3) Mechanical Pencil (cylinder + cone)

- Cylinder: $V = 3.14 \cdot 0.4^2 \cdot 17 = 8.5408 \text{ cm}^3$
 - Cone: $V = \frac{1}{3} \cdot 3.14 \cdot 0.3^2 \cdot 1.2 = 0.11304 \text{ cm}^3$
 - Total: $8.5408 + 0.11304 = \boxed{8.65 \text{ cm}^3}$
-

4) Bike Helmet Shell (outer hemisphere – inner hemisphere)

- Outer ($r = 14$): $V_o = \frac{2}{3} \cdot 3.14 \cdot 14^3 = 5,744.11 \text{ cm}^3$
 - Inner ($r = 13$): $V_i = \frac{2}{3} \cdot 3.14 \cdot 13^3 = 4,599.05 \text{ cm}^3$
 - Shell: $5,744.11 - 4,599.05 = \boxed{1,145.05 \text{ cm}^3}$
-

5) Entrance Planter (prism – rectangular void – 2 cylinders)

- Box: $V = 120 \cdot 40 \cdot 35 = 168,000 \text{ cm}^3$
- Rectangular void: $V = 60 \cdot 10 \cdot 10 = 6,000 \text{ cm}^3$
- One pipe: $V = 3.14 \cdot 3^2 \cdot 35 = 989.10 \text{ cm}^3 \Rightarrow$ Two pipes: $1,978.20 \text{ cm}^3$
- Soil capacity: $168,000 - 6,000 - 1,978.20 = \boxed{160,021.80 \text{ cm}^3} (\approx 160.02 \text{ L})$